



Ecosystem Gas Exchange: The Eddy Covariance Method

Liukang Xu

Outline

1. Basic eddy covariance (EC) theory
2. Examples of long-term flux measurements
3. GAP-filling
4. $GPP = R_{eco} - NEE$
5. Advantages of EC, and its disadvantages

Definition of variance and covariance

$x_1, x_2, x_3, x_4 \dots \dots \dots x_n$

$y_1, y_2, y_3, y_4 \dots \dots \dots y_n$

$$\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2 \text{ variance, 方差}$$

$$\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y}) = \overline{x'y'} \text{ covariance, 协方差}$$

Terminology and units for gas flux

CO₂ flux: $\mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$
 $\text{g C m}^{-2} \text{ d}^{-1}$
 $\text{g C m}^{-2} \text{ yr}^{-1}$

H₂O flux (E): $\text{mmol H}_2\text{O m}^{-2} \text{ s}^{-1}$
(ET): $\text{mm hr}^{-1}, \text{mm day}^{-1}$

CH₄ flux: $\text{nmol m}^{-2} \text{ s}^{-1}$

N₂O flux: $\text{nmol m}^{-2} \text{ s}^{-1}$

Terminology and units for energy flux

Net radiation (R_{net}): W m^{-2}

Sensible heat flux (H): W m^{-2} ($\text{J m}^{-2} \text{s}^{-1}$)

Latent heat flux (LE): $LE = \lambda E$ (W m^{-2})
(*E is water vapor flux*)

Soil heat flux (G): W m^{-2}

Vertical profile for environmental variables

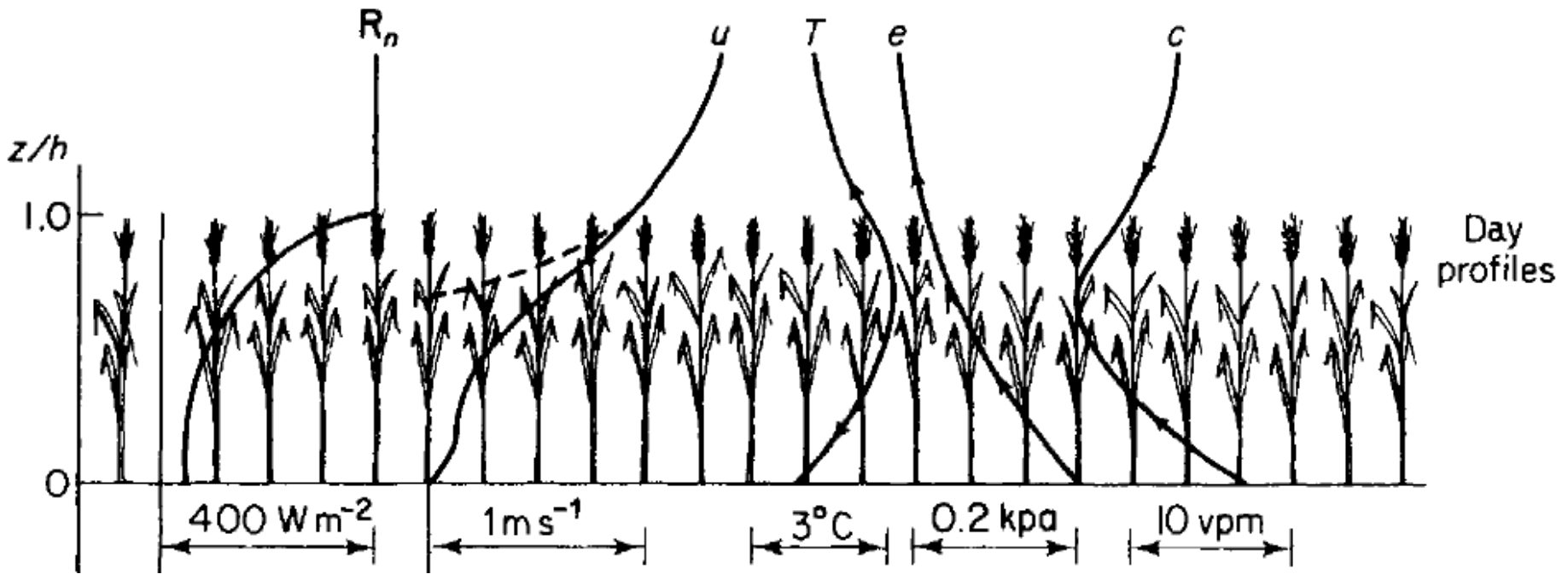
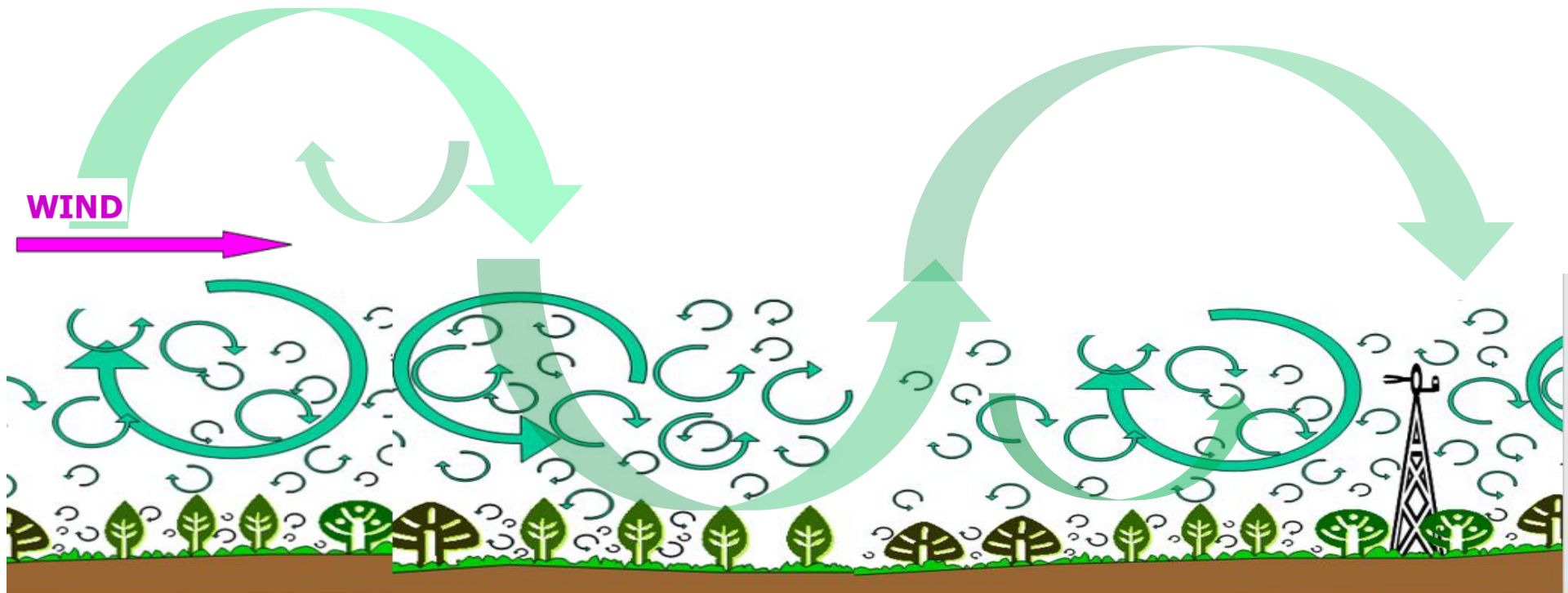
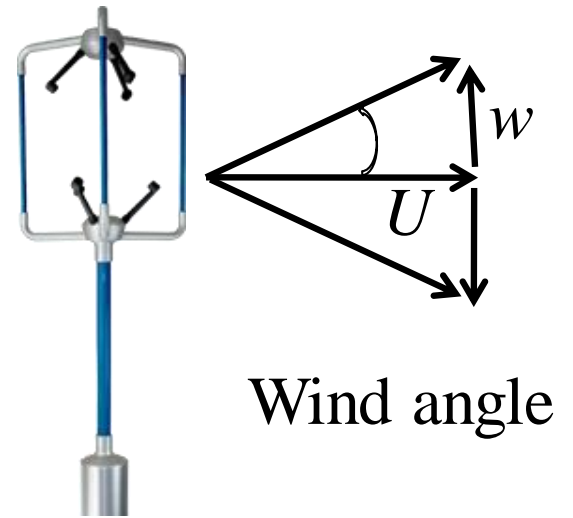


Fig. 16.5. Monteith and Unsworth, 2013. Environmental Physics.

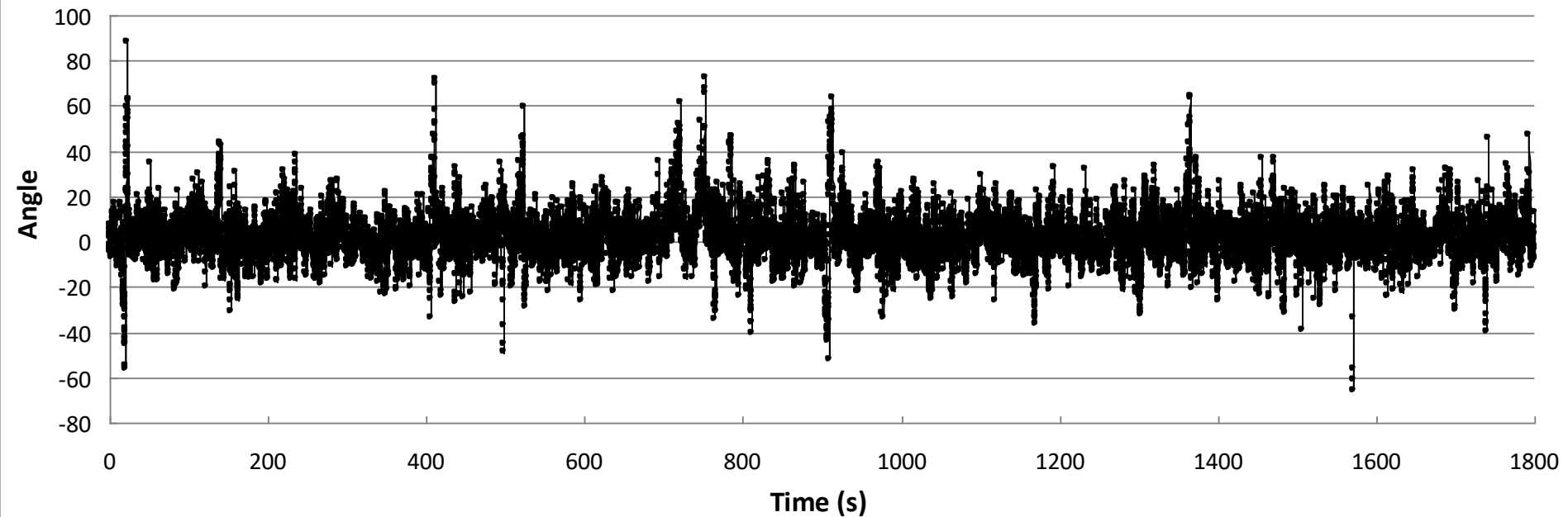
Eddy Covariance flux measurement



Here is more 10-Hz
raw data...



California Grassland 2 m tall tower, DOY104 1200

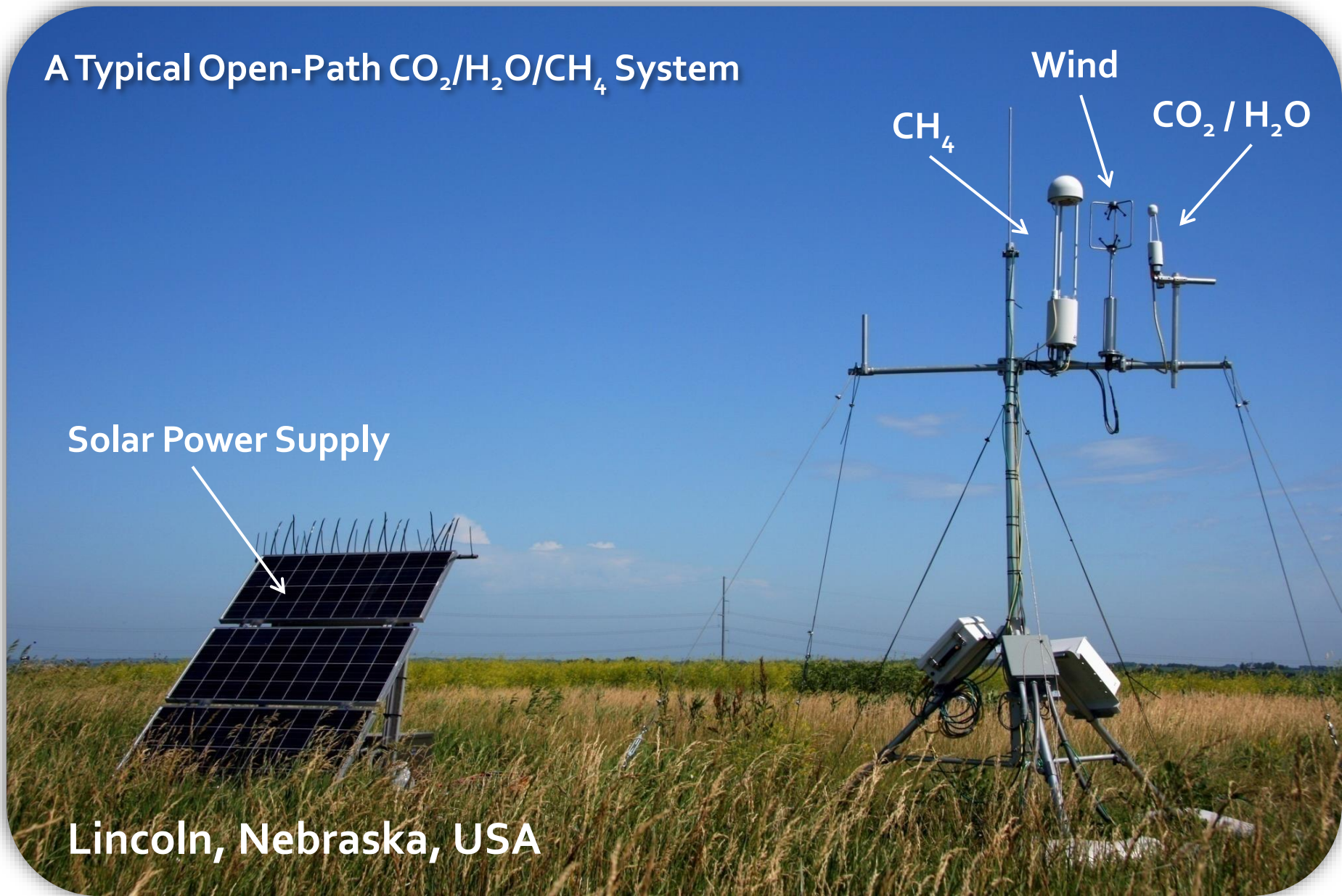


A Typical Open-Path $\text{CO}_2/\text{H}_2\text{O}/\text{CH}_4$ System

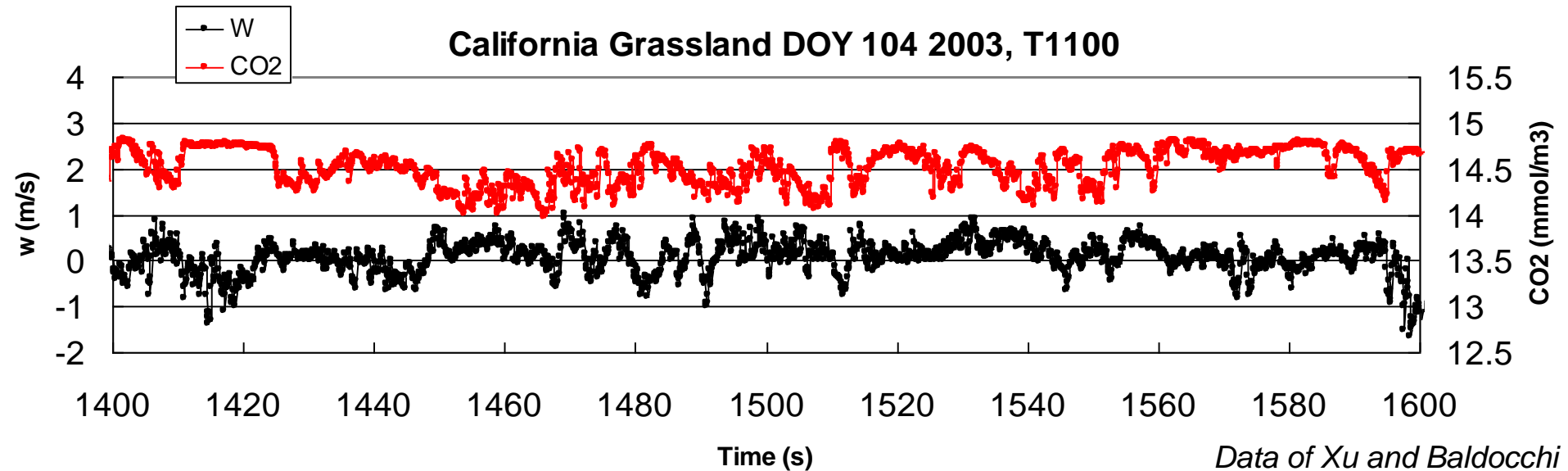
Solar Power Supply

CH_4 Wind $\text{CO}_2/\text{H}_2\text{O}$

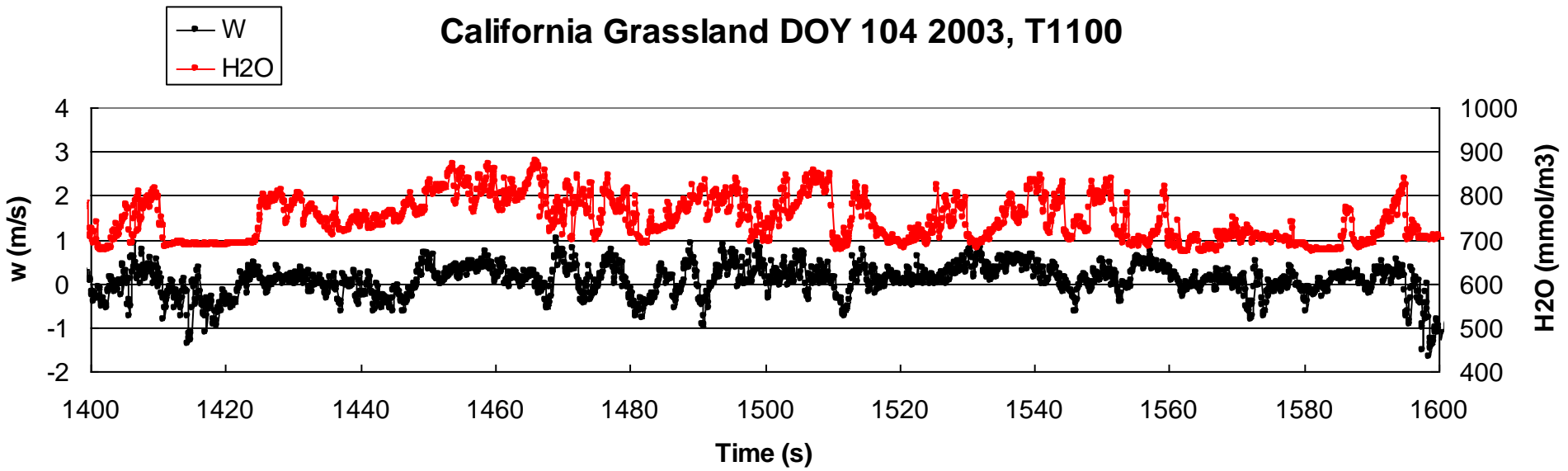
Lincoln, Nebraska, USA



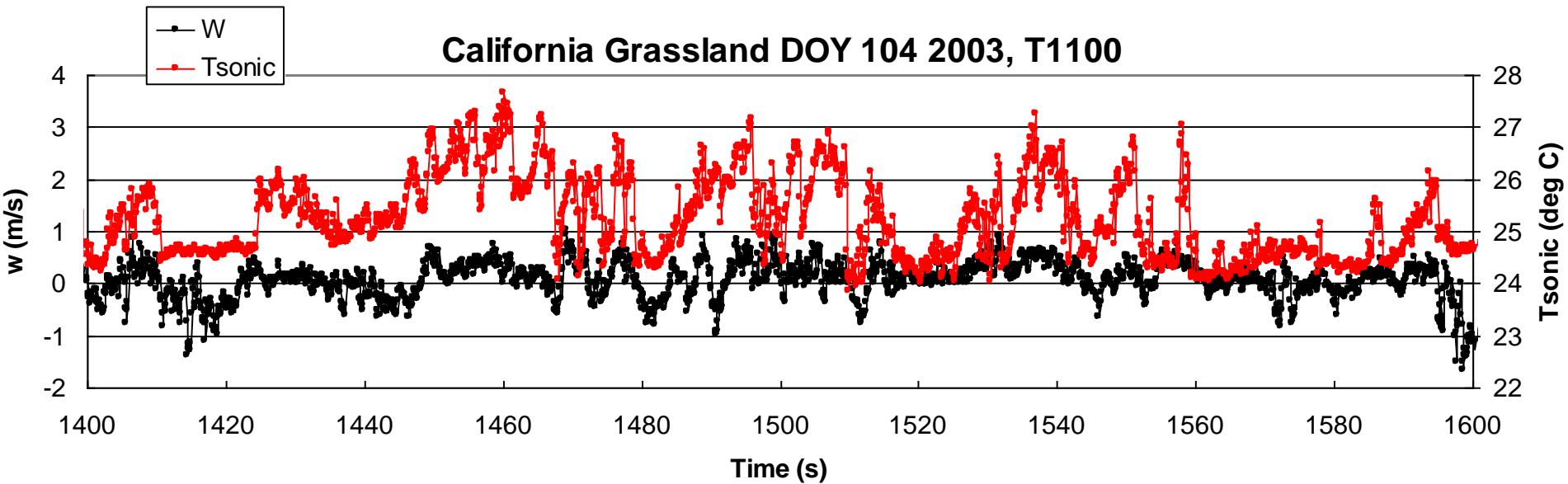
Let's see some
10-Hz real data!



California Grassland DOY 104 2003, T1100



California Grassland DOY 104 2003, T1100

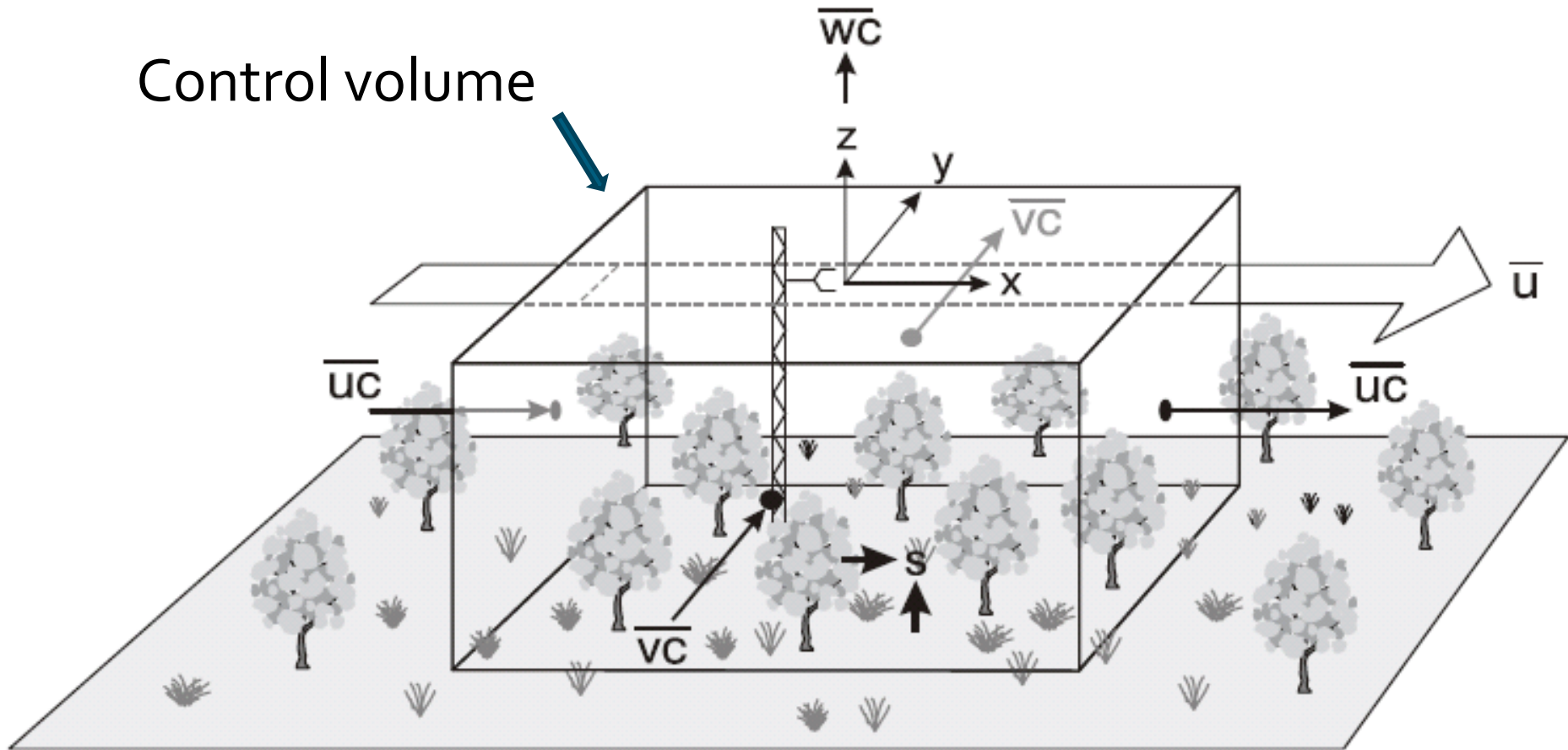


Basic assumptions:

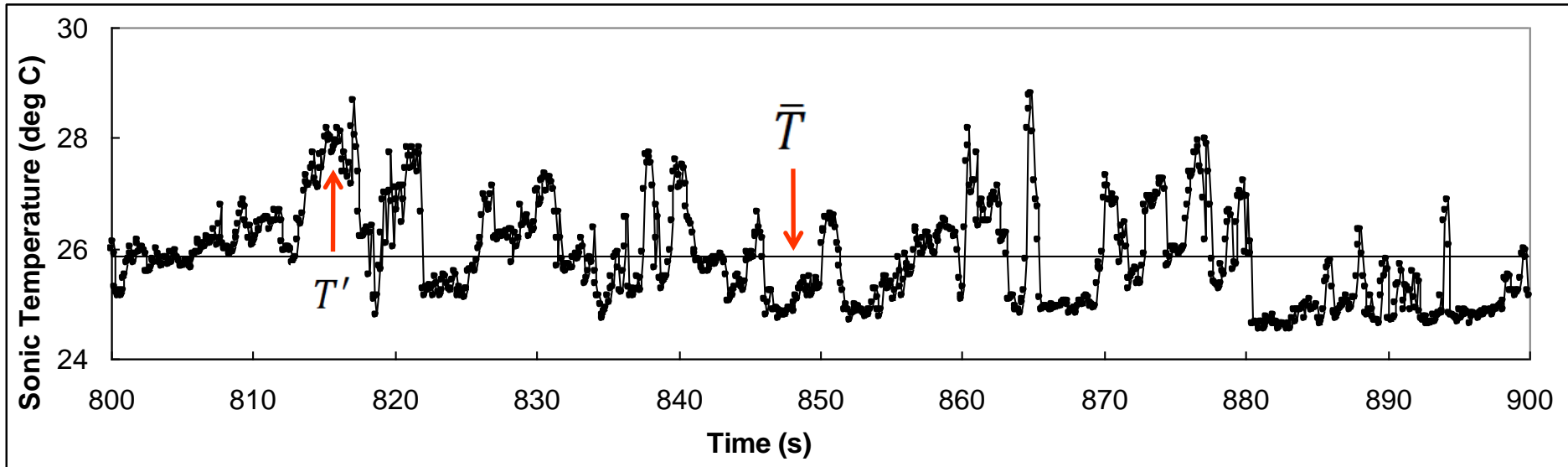
1. no horizontal divergence or convergence,

$$2. \frac{d\bar{C}}{dt} = 0$$

Control volume



Reynolds' Averaging Rules



$$x = \bar{x} + x' \quad \bar{x}' = 0$$

$$\overline{x + y} = \bar{x} + \bar{y}$$

$$\begin{aligned} \overline{xy} &= \overline{(\bar{x} + x')(\bar{y} + y')} = \overline{(\bar{x}\bar{y} + \bar{x}y' + x'\bar{y} + x'y')} \\ &= \overline{\bar{x}\bar{y}} + \overline{x'y'} \end{aligned}$$

EC theory: Complete equations

$$F = \overline{w c} \qquad F = \overline{(\overline{w} + w')(\overline{c} + c')}$$

$$F = \overline{\overline{w} \overline{c} + \overline{w} c' + w' \overline{c} + w' c'}$$

$\overline{w} = 0$ $\overline{w'} = 0$

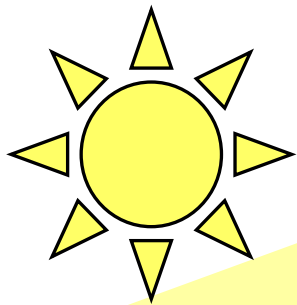
$$F = \overline{w' c'} = \frac{1}{18000} \sum_{i=1}^{18000} (w - \overline{w})(c - \overline{c})$$

$$\frac{m}{s} \times \frac{\mu\text{mol } CO_2}{m^3} = \frac{\mu\text{mol}}{m^2 s}$$

Density unit!



Time	CO ₂ (mmol m ⁻³)	W (m s ⁻¹)	CO ₂ '	W'	W'CO ₂ '		
0	15.511	-0.253	0.108	-0.253	-0.027		
0.1	15.483	-0.348	0.080	-0.348	-0.028		
0.2	15.442	-0.290	0.039	-0.290	-0.011		
0.3	15.420	-0.052	0.017	-0.052	-0.001		
0.4	15.414	0.091	0.012	0.091	0.001		
0.5	15.409	0.159	0.006	0.159	0.001		
0.6	15.401	0.276	-0.002	0.276	-0.001		
0.7	15.407	0.401	0.004	0.401	0.002		
0.8	15.403	0.496	0.001	0.496	0.000		
.		
.		
1800	15.369	0.212	-0.034	0.212	-0.007		
mean	15.403	0.000				$\overline{w'CO_2'} =$	-0.014 (mmol m ⁻² s ⁻¹)

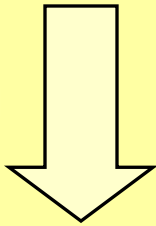


EC for energy flux measurement

$$H = \rho_a C_p \overline{w'T'} = \frac{g \text{ air}}{m^3} \times \frac{J}{g \text{ air} \cdot C} \times \frac{m}{s} \times C = \frac{J}{m^2 s} = \frac{W}{m^2}$$

$$LE = L \rho_a \overline{w'q'} = \frac{J}{g \text{ H}_2\text{O}} \times \frac{g \text{ air}}{m^3} \times \frac{m}{s} \times \frac{g \text{ H}_2\text{O}}{g \text{ air}} = \frac{J}{m^2 s} = \frac{W}{m^2}$$

Rn



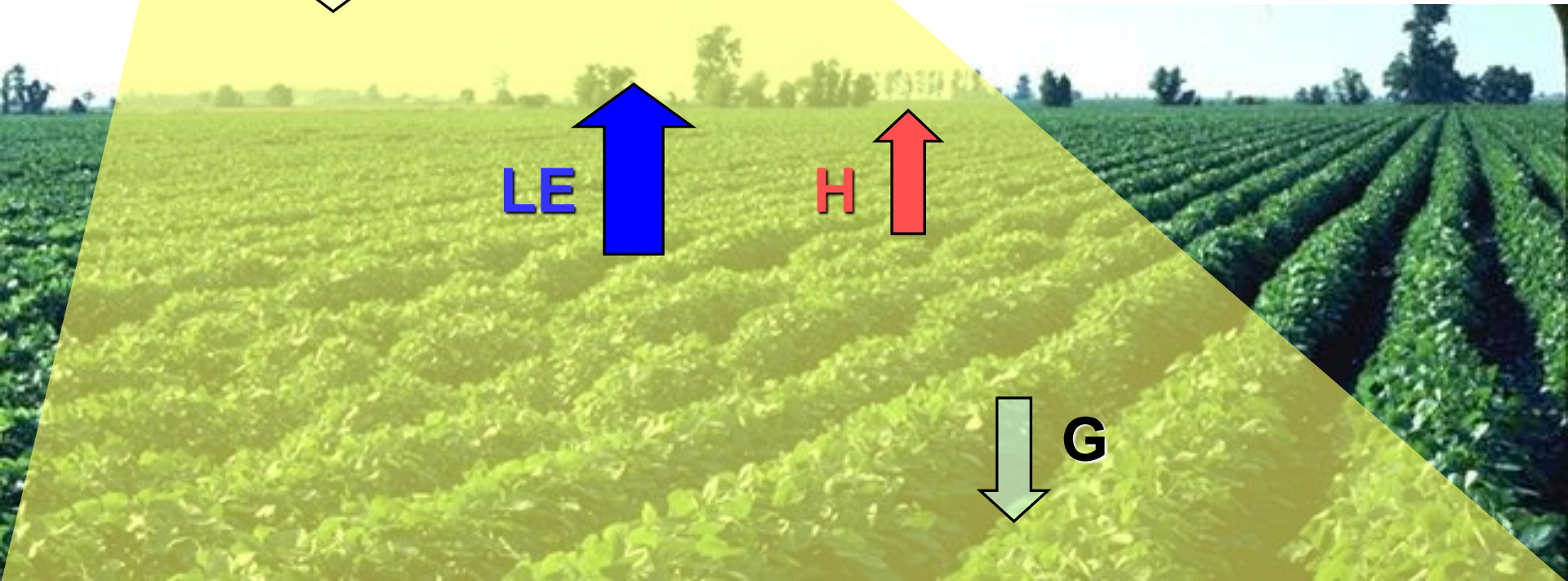
LE



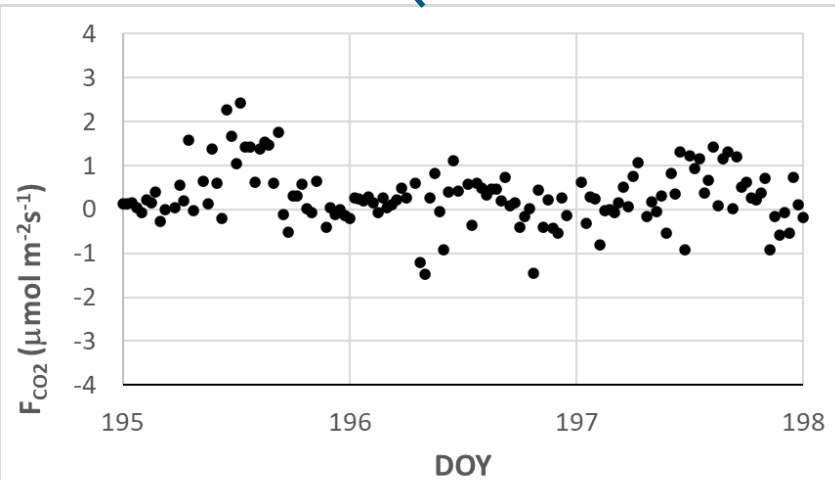
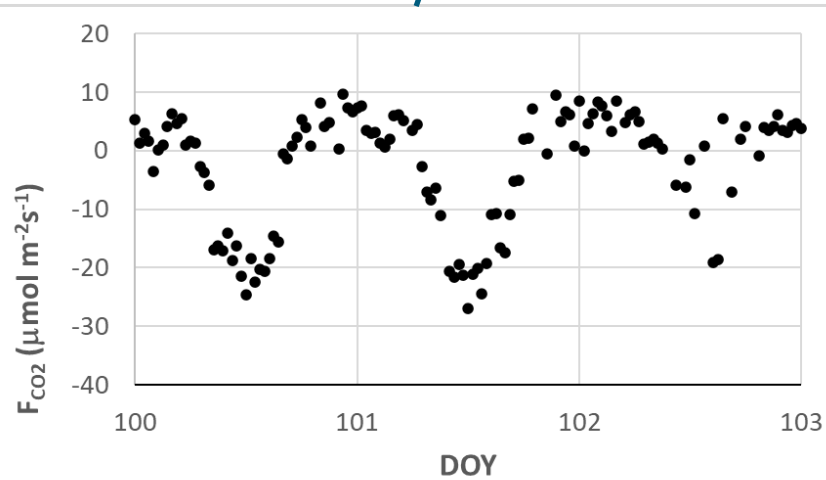
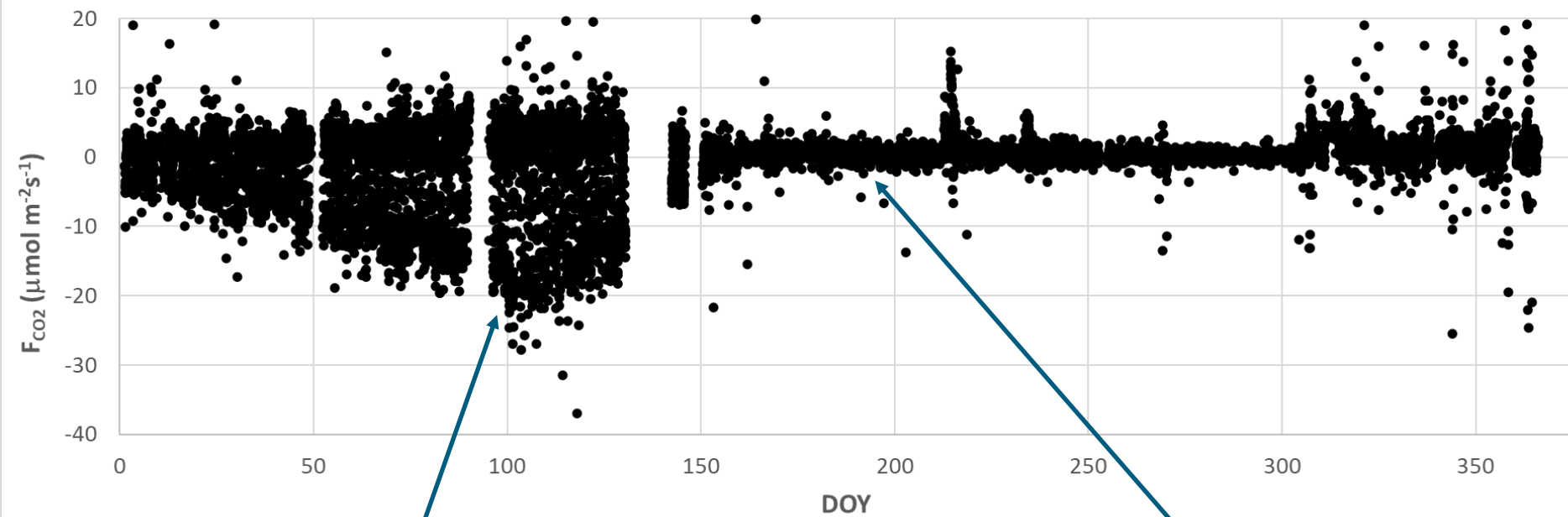
H



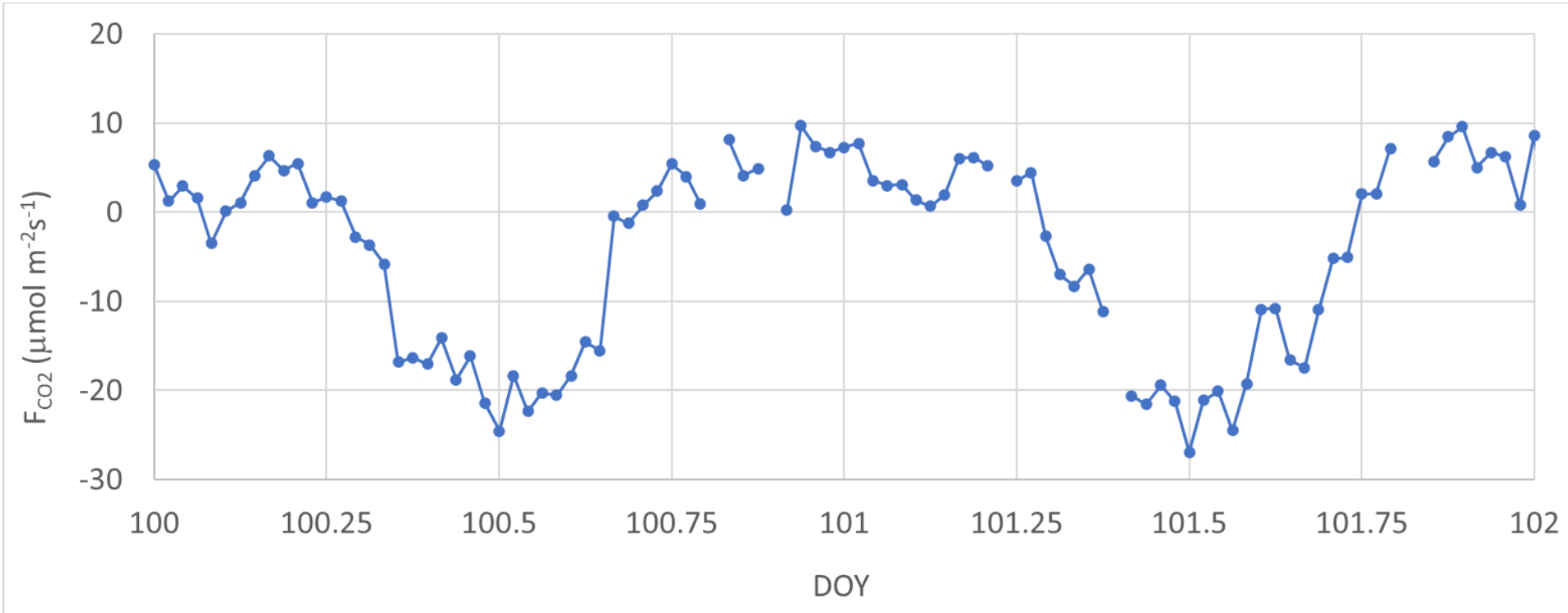
G



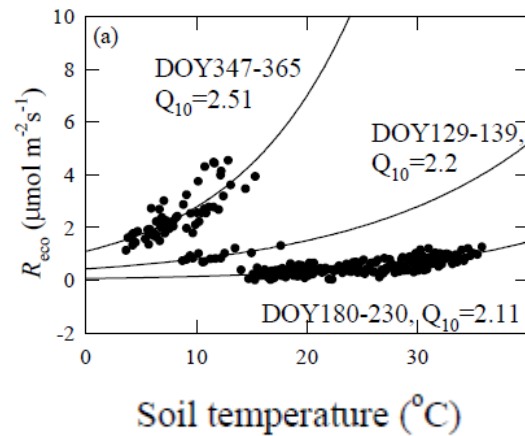
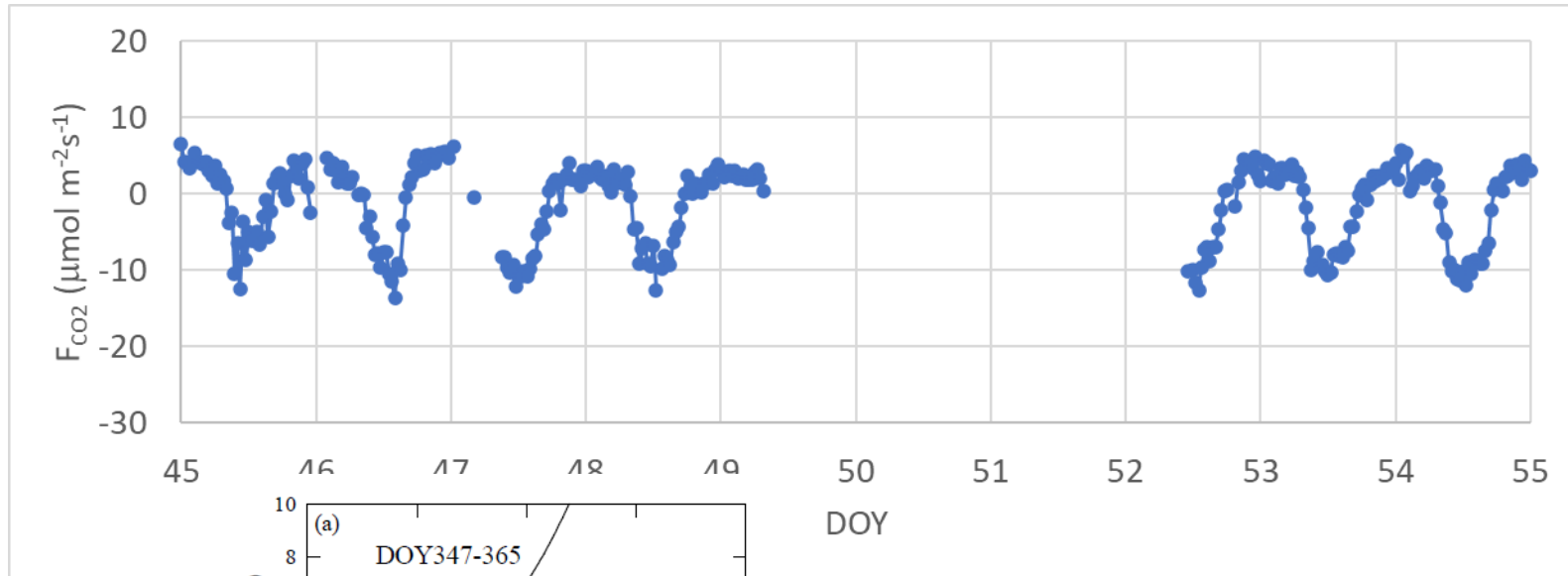
CO₂ flux from a California Grassland (2003)



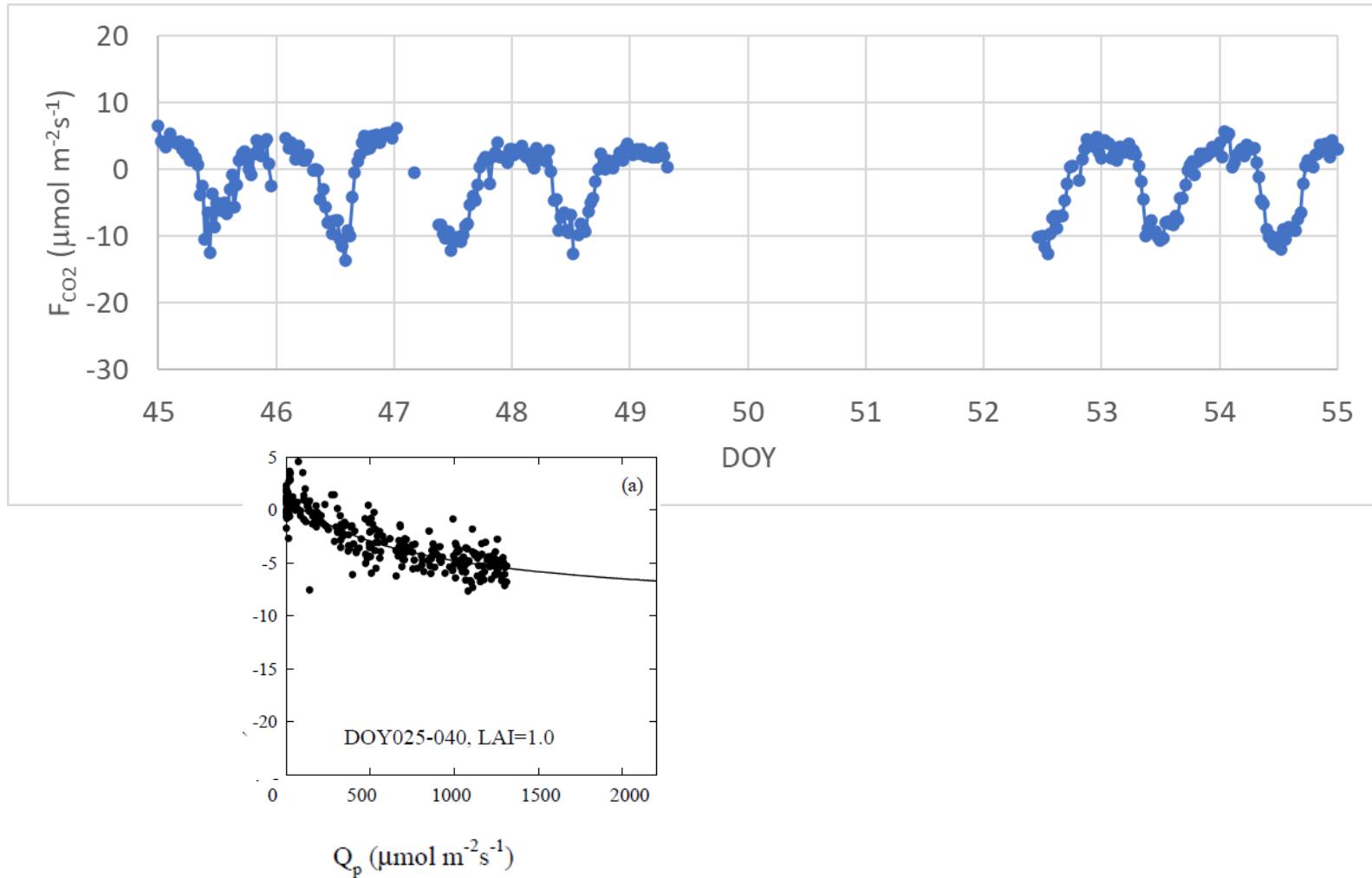
Gap filling for short time



Gap filling nighttime flux data

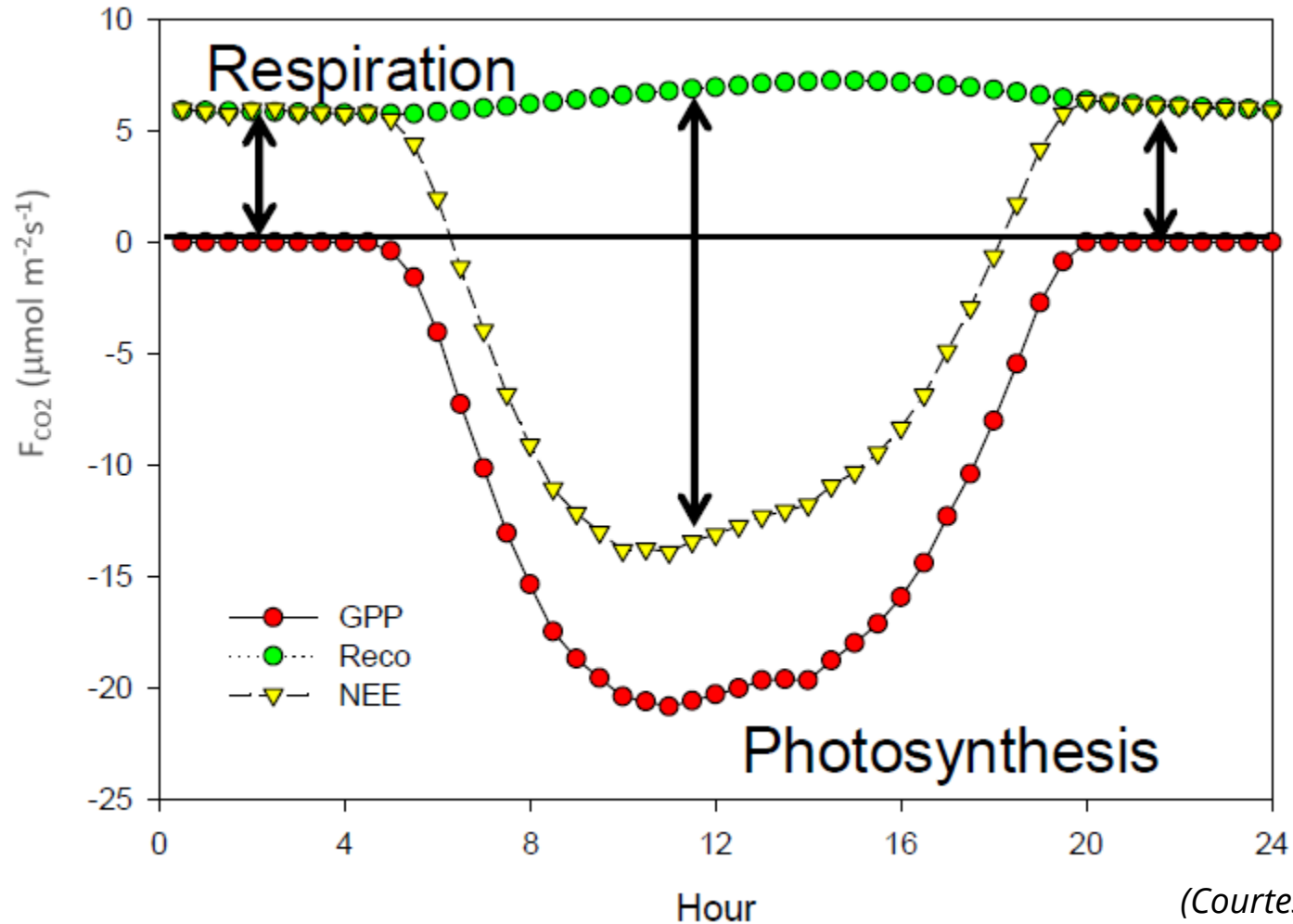


Gap filling daytime flux data



GPP estimation

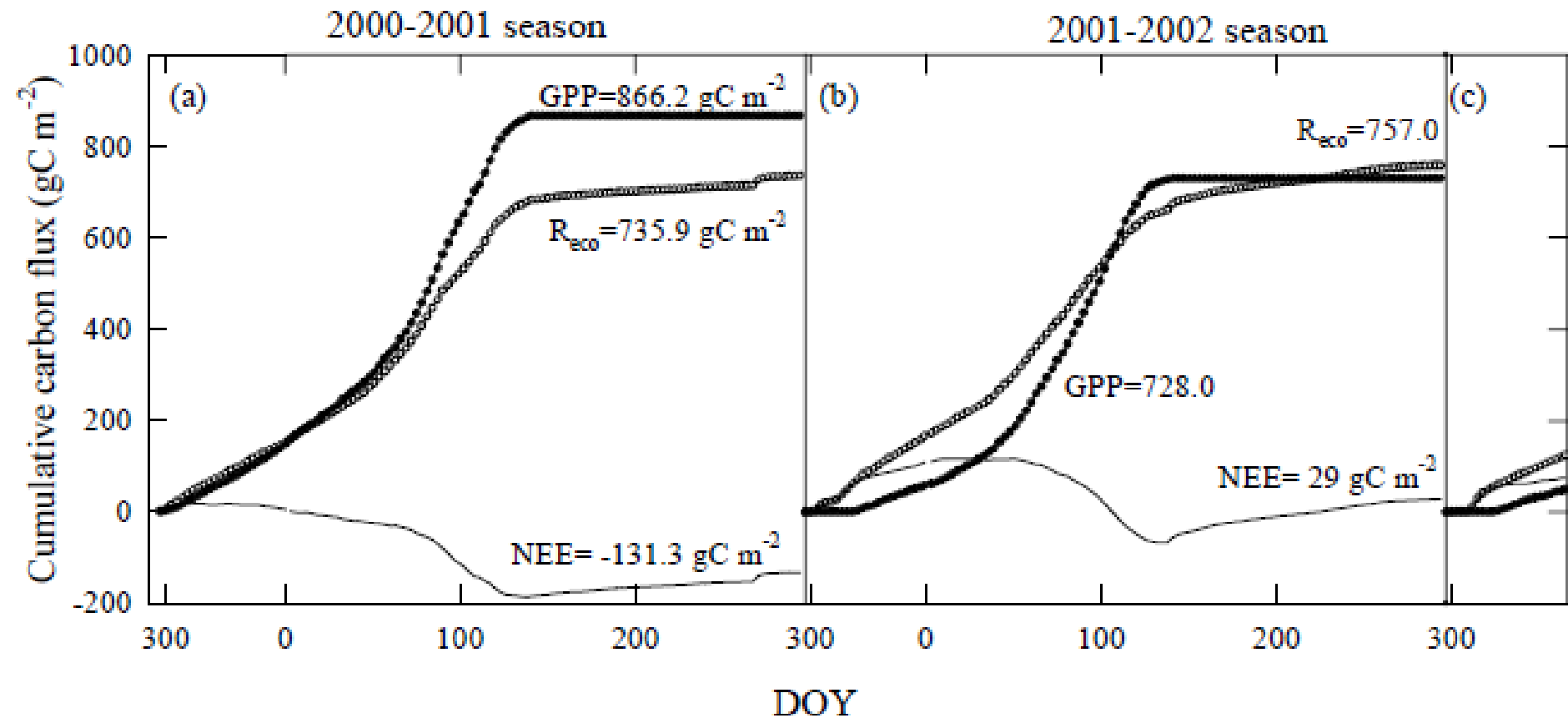
$$GPP = R_{eco} - NEE$$



(Courtesy of Dr. Baldocchi)

Example of long-term flux data (2000-2003) California grassland

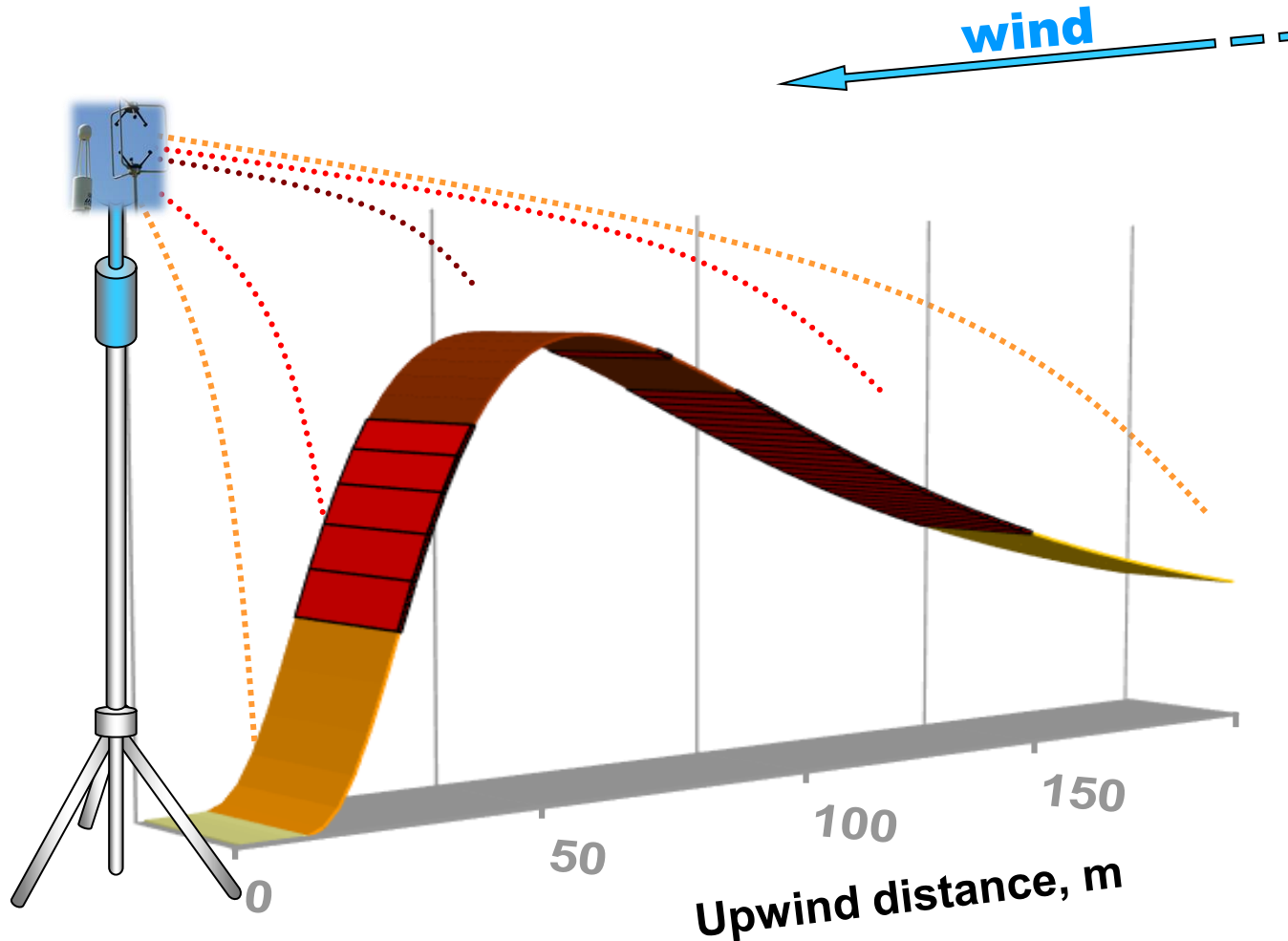
L. Xu, D.D. Baldocchi / Agricultural and Forest Meteorology 1232 (2004) 79–96



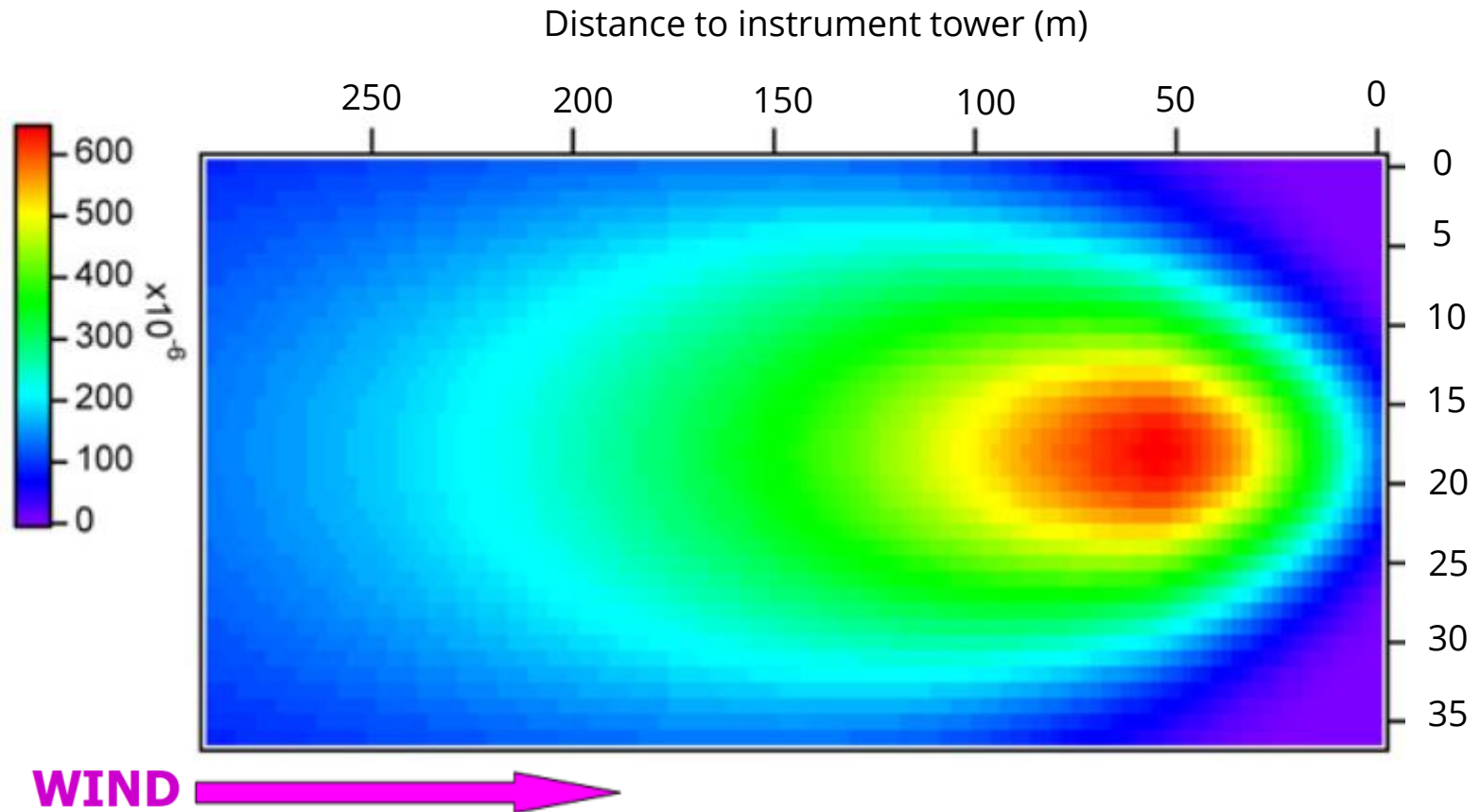


No disturbance to your ecosystem: $> 10,000 \text{ m}^2$

The footprint is defined as the relative contribution at different location (in the upwind direction) to the measured vertical flux



Footprint of EC measurement-2D



Advantages of the EC Method

1. Direct measure of the flux density
2. *in situ*
3. No disturbance to your ecosystem
4. Continuous
5. Represents a large upwind area

Disadvantages of the EC Method

1. Nighttime low turbulent conditions
2. Complex terrain affects your measurement
3. Cannot be used over a small area

Summary

1. Eddy covariance theory – Basic micrometeorology theory
2. Examples of long-term flux measurements
3. Gap filling
4. $GPP = R_{eco} - NEE$
5. Advantages of EC method

Q & A